

2) The Durbin Watson test of the multiple regression, the model is

$$Y_t = \beta_0 + \beta_1 X_{t1} + \beta_2 X_{t2} + \dots + \beta_p X_{tp} + \varepsilon_t, t = 1, 2, \dots, T, p \geq 2, T - (p + 1) \geq 1,$$

$$\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\varepsilon},$$

assumption:

$$(1) E(\boldsymbol{\varepsilon}) = \mathbf{0}, \quad (2) E(\mathbf{X}^T \boldsymbol{\varepsilon}) = \mathbf{0}, \quad (3) \varepsilon_t \sim N(0, \sigma_\varepsilon^2), \quad E(\boldsymbol{\varepsilon}\boldsymbol{\varepsilon}^T) = \sigma_\varepsilon^2 \times \begin{bmatrix} 1 & \rho & 0 & \dots & 0 \\ \rho & 1 & \rho & \dots & 0 \\ \dots & \rho & 1 & \dots & 0 \\ \dots & \dots & \dots & \dots & \rho \\ 0 & 0 & \dots & \rho & 1 \end{bmatrix}$$

$$\boldsymbol{\varepsilon} = \mathbf{Y} - \mathbf{X}\boldsymbol{\beta}, \quad \boldsymbol{\varepsilon}\boldsymbol{\varepsilon}^T = (\mathbf{Y} - \mathbf{X}\boldsymbol{\beta})^T (\mathbf{Y} - \mathbf{X}\boldsymbol{\beta}), \quad \frac{\partial(\boldsymbol{\varepsilon}\boldsymbol{\varepsilon}^T)}{\partial \boldsymbol{\beta}} = \mathbf{0}, \quad \hat{\boldsymbol{\beta}} = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{Y},$$

$$\hat{\mathbf{Y}} = \mathbf{X}\hat{\boldsymbol{\beta}} = \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{Y}, \quad \mathbf{e} = \mathbf{Y} - \hat{\mathbf{Y}} = \mathbf{Y} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{Y},$$

The constrains are $\mathbf{e}^T \mathbf{X} = \mathbf{0}$ and the degree of freedom is T-p-1.

But the collinearity of independent variables is a condition of $\mathbf{e}^T \mathbf{X} = \mathbf{0}$.

$\mathbf{e} = (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T) \mathbf{Y}$, the error variance-covariance matrix is

$$E(\boldsymbol{\varepsilon}\boldsymbol{\varepsilon}^T) = E[(\mathbf{Y} - \mathbf{X}\boldsymbol{\beta})(\mathbf{Y} - \mathbf{X}\boldsymbol{\beta})^T] = E(\mathbf{Y}\mathbf{Y}^T) - \mathbf{X}\boldsymbol{\beta}E(\mathbf{Y}^T) - E(\mathbf{Y})\boldsymbol{\beta}^T \mathbf{X}^T$$

$$+ \mathbf{X}\boldsymbol{\beta}\boldsymbol{\beta}^T \mathbf{X}^T = E(\mathbf{Y}\mathbf{Y}^T) - \mathbf{X}\boldsymbol{\beta}\boldsymbol{\beta}^T \mathbf{X}^T, \quad E(\mathbf{Y}\mathbf{Y}^T) = \sigma_\varepsilon^2 \times \begin{bmatrix} 1 & \rho & 0 & \dots & 0 \\ \rho & 1 & \rho & \dots & 0 \\ \dots & \rho & 1 & \dots & 0 \\ \dots & \dots & \dots & \dots & \rho \\ 0 & 0 & \dots & \rho & 1 \end{bmatrix} + \mathbf{X}\boldsymbol{\beta}\boldsymbol{\beta}^T \mathbf{X}^T$$

$$\begin{aligned}
E(\mathbf{ee}^T) &= (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T) E(\mathbf{Y}\mathbf{Y}^T) (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T)^T \\
&= (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T) \left(\sigma_\varepsilon^2 \times \begin{bmatrix} 1 & \rho & 0 & \dots & 0 \\ \rho & 1 & \rho & \dots & 0 \\ \dots & \rho & 1 & \dots & 0 \\ \dots & \dots & \dots & \dots & \rho \\ 0 & 0 & \dots & \rho & 1 \end{bmatrix} + \mathbf{X}\boldsymbol{\beta}\boldsymbol{\beta}^T \mathbf{X}^T \right) (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T)^T \\
&= (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T) \left(\sigma_\varepsilon^2 \times \begin{bmatrix} 1 & \rho & 0 & \dots & 0 \\ \rho & 1 & \rho & \dots & 0 \\ \dots & \rho & 1 & \dots & 0 \\ \dots & \dots & \dots & \dots & \rho \\ 0 & 0 & \dots & \rho & 1 \end{bmatrix} \right) (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T)^T \\
&= \sigma_\varepsilon^2 \times (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T) \begin{bmatrix} 1 & \rho & 0 & \dots & 0 \\ \rho & 1 & \rho & \dots & 0 \\ \dots & \rho & 1 & \dots & 0 \\ \dots & \dots & \dots & \dots & \rho \\ 0 & 0 & \dots & \rho & 1 \end{bmatrix} (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T)^T
\end{aligned}$$

if $\rho = 0$, $E(\mathbf{ee}^T) = \sigma_\varepsilon^2 \times (\mathbf{I} - \mathbf{X}(\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T)$

$$H_0 : \rho = \rho_0, H_1 : \rho \neq \rho_0, \text{New } D.W. = \frac{\sum_{t=2}^T (e_t \times e_{t-1})}{\sum_{t=1}^T e_t^2},$$

New $D.W. < W_{1-\alpha/2}$ or New $D.W. > W_{\alpha/2} \Rightarrow \text{reject } H_0$

$$H_0 : \rho \leq \rho_0, H_1 : \rho > \rho_0, \text{New } D.W. = \frac{\sum_{t=2}^T (e_t \times e_{t-1})}{\sum_{t=1}^T e_t^2},$$

New $D.W. > W_\alpha \Rightarrow \text{reject } H_0$

$$H_0 : \rho \geq \rho_0, H_1 : \rho < \rho_0, \text{New } D.W. = \frac{\sum_{t=2}^T (e_t \times e_{t-1})}{\sum_{t=1}^T e_t^2},$$

New $D.W. < W_{1-\alpha} \Rightarrow \text{reject } H_0$

2.1).same independent variable value, but auto correlation coefficient is different:

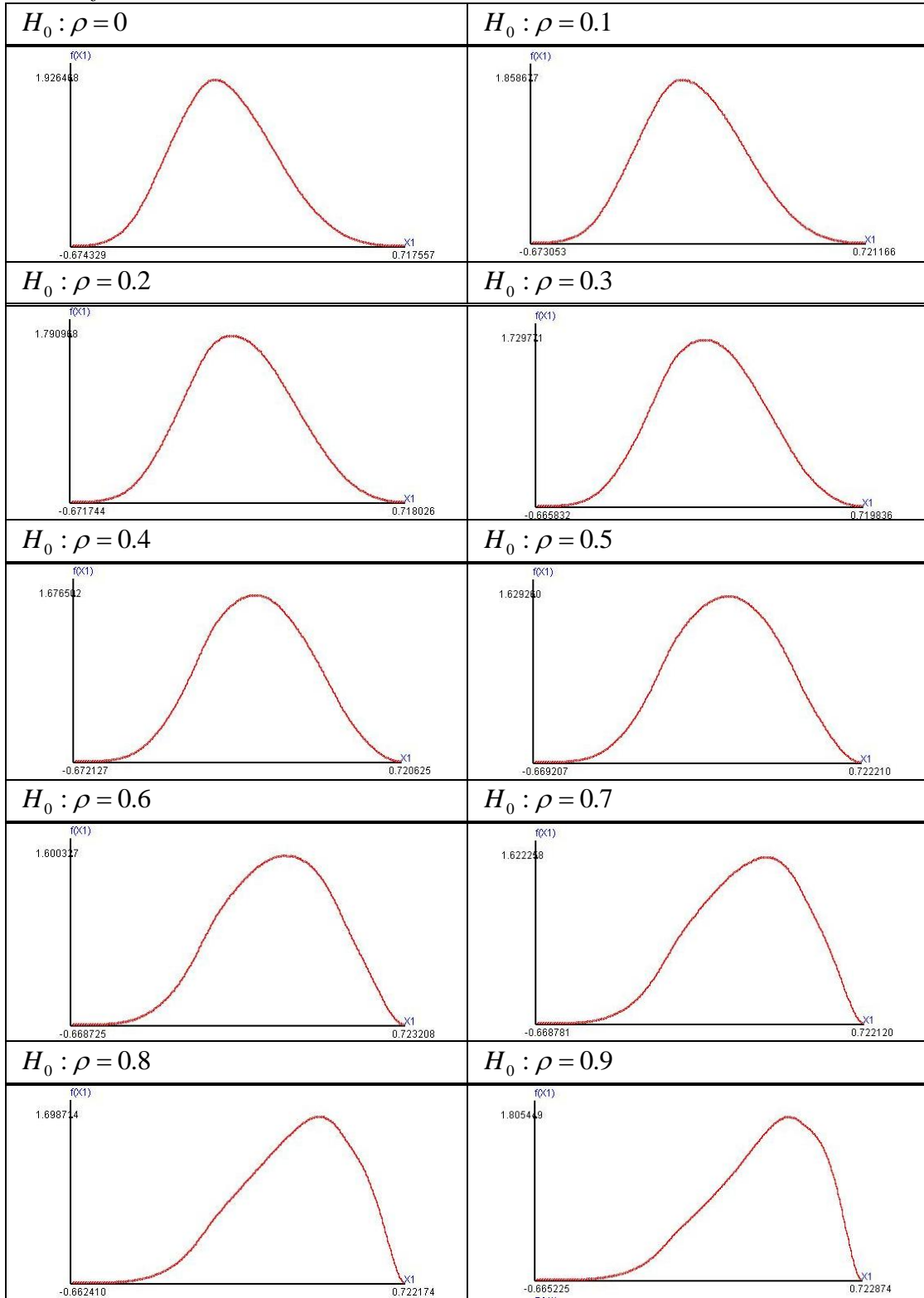
2.1.1)Case 1:

	X1	X2	X3
X4	X5	X6	
1 :	54.2327801017,	-1.0515635183,	-2.6129142144,
95.8729376089,	22.6710077518,	-0.2330759733,	
2 :	13.9250244388,	4.5308629808,	-2.8927090373,
89.5992578910,	8.9801011409,	-2.0197242513,	
3 :	14.6498749197,	1.6952356061,	-7.4321385213,
90.7336550626,	32.0067903020,	0.4088939995,	
4 :	7.9783225134,	1.7818026806,	-6.5196035366,
109.1869631249,	8.9810690255,	0.1523776054,	
5 :	8.6762253740,	8.1590653669,	-3.0465392653,
102.2317225115,	14.2386734597,	0.1328963108,	
6 :	27.7623540858,	1.2328513211,	-8.4102613007,
84.5890555624,	9.2839680305,	0.6524649479,	
7 :	18.6625587758,	3.2933744224,	-4.0086189009,
63.8968287439,	3.2012130715,	0.3515600164,	
8 :	39.3319153828,	7.0312539167,	-4.8855110925,
124.8773844220,	14.6127561535,	0.8325246655,	
9 :	17.9656598313,	-0.1333539865,	-5.5127281095,
85.5531179580,	15.7406949223,	-3.0863445859,	
10 :	32.0610021717,	3.4854361980,	-1.7108106596,
86.1964533707,	4.1842050838,	-1.7323733277,	
11 :	13.7528011906,	-4.6549833265,	-3.9099059591,
91.5492024874,	7.8007722665,	-0.4902037820,	
12 :	28.2464630681,	7.9737622105,	-2.8270247690,
78.6405322222,	14.3222964868,	0.6649429561,	
13 :	13.0932431125,	1.1946253885,	-8.9544367518,
113.4092231132,	14.0899356091,	1.8632771636,	
14 :	20.4243954765,	-3.9039174396,	-5.3385220478,
138.7602214818,	6.0689637971,	-2.3724228711,	
15 :	22.6946305148,	11.6094138960,	-1.6969031058,
119.8805947892,	10.5394804672,	-0.1477014572,	

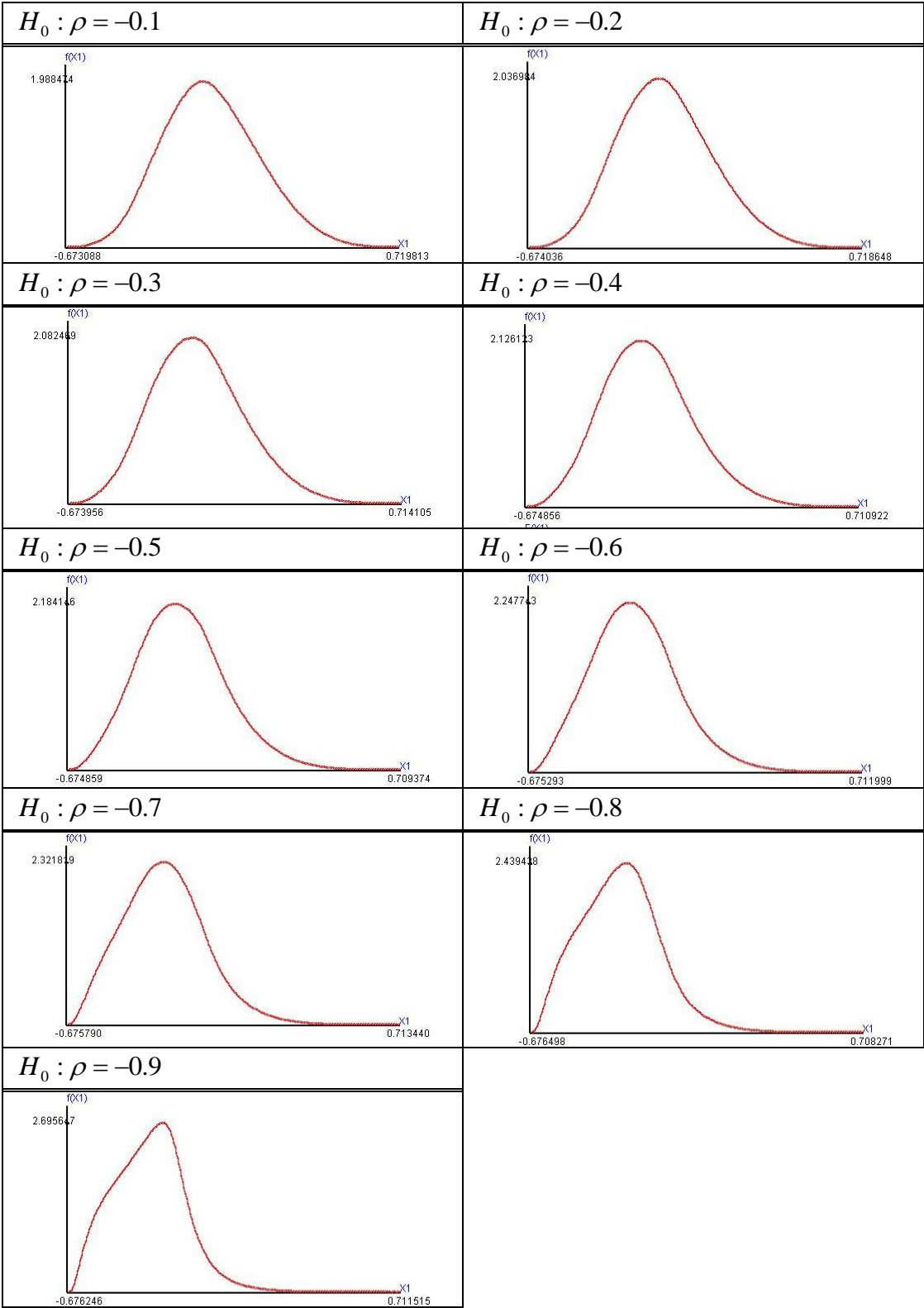
indepdent sample correlation coefficient-----

	X1	X2	X3	X4	X5
X2	0.024028234	1			
X3	0.314646678	0.405194595	1		
X4	0.005269787	0.001539342	-0.131205559	1	
X5	0.182811853	0.017165054	-0.249082423	0.011680009	1
X6	0.043103752	0.309836262	-0.358269997	-0.005317961	0.246722421

$T=15, df=15-7=8,$



The probability distribution of Durbin Watson test will be modified when the autocorrelation coefficient changed.



Coefficeint:

Hypothesis	Average	Variance	Coefficient of Skewed	Coefficient of Kurtosis
$H_0 : \rho = 0$	-0.03635	0.04155	0.21133	2.75464
$H_0 : \rho = 0.1$	-0.00289	0.04299	0.15934	2.69259
$H_0 : \rho = 0.2$	0.03127	0.04448	0.10492	2.63624
$H_0 : \rho = 0.3$	0.06660	0.04603	0.04662	2.58404
$H_0 : \rho = 0.4$	0.10352	0.04759	-0.01827	2.53666
$H_0 : \rho = 0.5$	0.14236	0.04906	-0.09338	2.49929
$H_0 : \rho = 0.6$	0.18309	0.05018	-0.18247	2.48332
$H_0 : \rho = 0.7$	0.22498	0.05062	-0.28815	2.50586
$H_0 : \rho = 0.8$	0.26627	0.04997	-0.41054	2.58608
$H_0 : \rho = 0.9$	0.30397	0.04799	-0.54683	2.73837
$H_0 : \rho = -0.1$	-0.06949	0.04011	0.26101	2.82416
$H_0 : \rho = -0.2$	-0.10266	0.03864	0.30734	2.90165
$H_0 : \rho = -0.3$	-0.13610	0.03711	0.34830	2.98520
$H_0 : \rho = -0.4$	-0.16998	0.03549	0.38129	3.06972
$H_0 : \rho = -0.5$	-0.20436	0.03375	0.40370	3.14718
$H_0 : \rho = -0.6$	-0.23913	0.03183	0.41348	3.20847
$H_0 : \rho = -0.7$	-0.27401	0.02961	0.40925	3.24774
$H_0 : \rho = -0.8$	-0.30842	0.02676	0.38943	3.27465
$H_0 : \rho = -0.9$	-0.34149	0.02233	0.34910	3.35497

Critical value:

Hypothesis	$1-\alpha$			
	0.995	0.99	0.975	0.95
$H_0 : \rho = 0$	-0.4988827775	-0.4625633263	-0.4065223647	-0.3561545040
$H_0 : \rho = 0.1$	-0.4794917870	-0.4416429821	-0.3838847121	-0.3317187818
$H_0 : \rho = 0.2$	-0.4601839632	-0.4209879838	-0.3612754288	-0.3068061403
$H_0 : \rho = 0.3$	-0.4408965871	-0.4002594134	-0.3381001589	-0.2809768431
$H_0 : \rho = 0.4$	-0.4212613761	-0.3789568039	-0.3137781191	-0.2538187607
$H_0 : \rho = 0.5$	-0.4009485914	-0.3566435526	-0.2879053060	-0.2250550601
$H_0 : \rho = 0.6$	-0.3795578137	-0.3328208812	-0.2601519910	-0.1945037189
$H_0 : \rho = 0.7$	-0.3567744263	-0.3071861835	-0.2305646169	-0.1624789086
$H_0 : \rho = 0.8$	-0.3324885371	-0.2799056798	-0.1996358124	-0.1296007225
$H_0 : \rho = 0.9$	-0.3071142486	-0.2518154721	-0.1684772052	-0.0969657237
$H_0 : \rho = -0.1$	-0.5181850590	-0.4840446562	-0.4296107207	-0.3805822395
$H_0 : \rho = -0.2$	-0.5375330474	-0.5057976700	-0.4536169292	-0.4056614788
$H_0 : \rho = -0.3$	-0.5566299386	-0.5276992002	-0.4786301683	-0.4317998222
$H_0 : \rho = -0.4$	-0.5750648632	-0.5493564831	-0.5042954202	-0.4593697318
$H_0 : \rho = -0.5$	-0.5925897401	-0.5701699907	-0.5298632296	-0.4880369054
$H_0 : \rho = -0.6$	-0.6085021101	-0.5894895783	-0.5543399768	-0.5165175843
$H_0 : \rho = -0.7$	-0.6221260127	-0.6062949813	-0.5763838729	-0.5431701180
$H_0 : \rho = -0.8$	-0.6325214202	-0.6193885968	-0.5942884407	-0.5656196419
$H_0 : \rho = -0.9$	-0.6381663671	-0.6268411747	-0.6049864343	-0.5795918600

Hypothesis	α			
	0.05	0.025	0.01	0.005
$H_0 : \rho = 0$	0.3164919019	0.3822230623	0.4536171911	0.4991639466
$H_0 : \rho = 0.1$	0.3526217925	0.4159808565	0.4843354511	0.5269766493
$H_0 : \rho = 0.2$	0.3889141140	0.4498443632	0.5148145553	0.5539417174
$H_0 : \rho = 0.3$	0.4257247843	0.4841693592	0.5446166618	0.5797390432
$H_0 : \rho = 0.4$	0.4632160559	0.5184869819	0.5730999049	0.6039731304
$H_0 : \rho = 0.5$	0.5010368483	0.5515563306	0.5995569466	0.6259347863
$H_0 : \rho = 0.6$	0.5372683194	0.5818357343	0.6229358414	0.6449578002
$H_0 : \rho = 0.7$	0.5694257384	0.6076285763	0.6420081193	0.6602635625
$H_0 : \rho = 0.8$	0.5947540970	0.6270080698	0.6557523248	0.6709843134
$H_0 : \rho = 0.9$	0.6108663694	0.6384178282	0.6632641597	0.6766143926
$H_0 : \rho = -0.1$	0.2800865773	0.3479697090	0.4225129072	0.4702088547
$H_0 : \rho = -0.2$	0.2428012225	0.3126850622	0.3904047796	0.4402138400
$H_0 : \rho = -0.3$	0.2041757246	0.2757432835	0.3564529836	0.4086172275

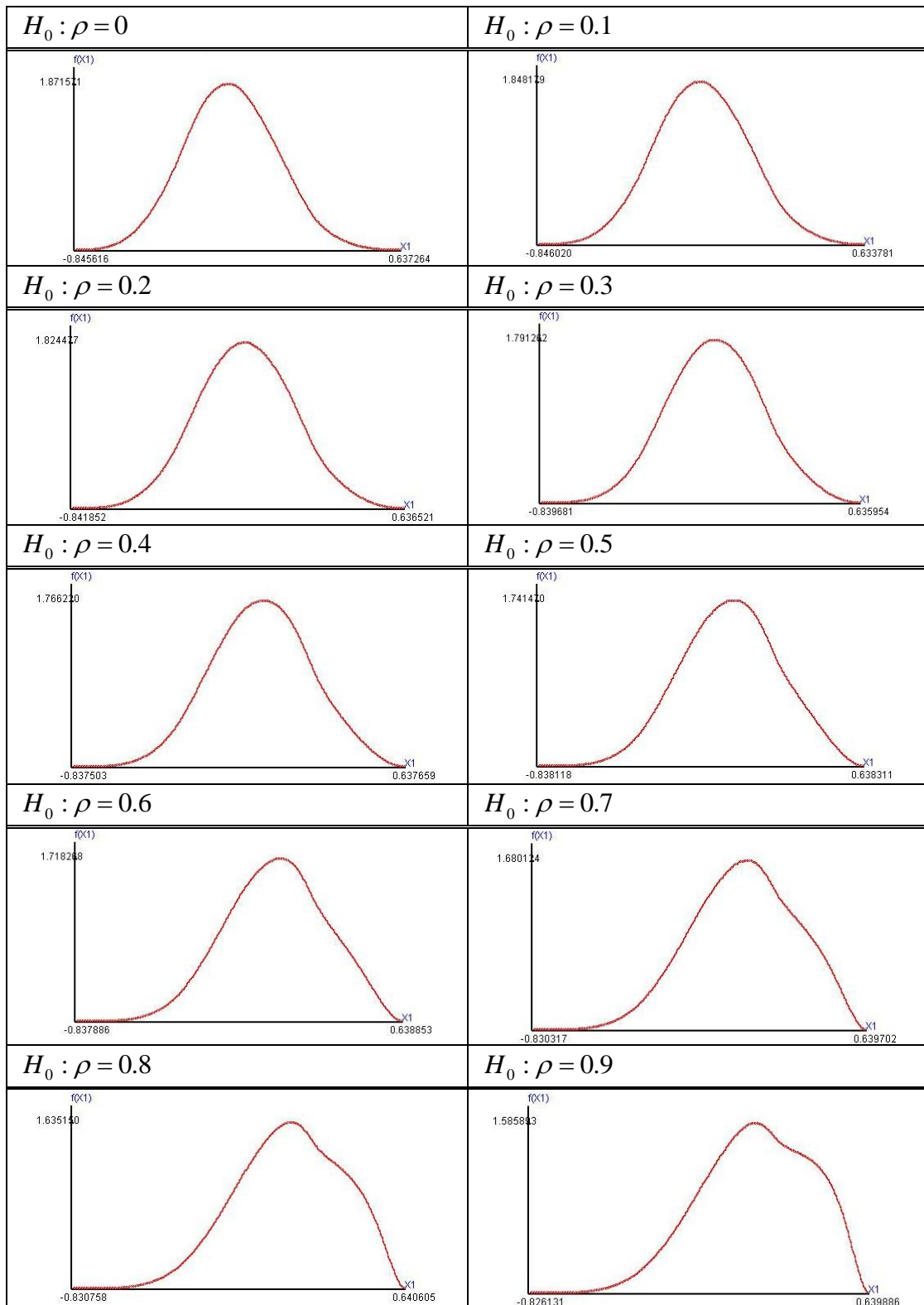
$H_0 : \rho = -0.4$	0.1634474423	0.2362775920	0.3198516742	0.3746206970
$H_0 : \rho = -0.5$	0.1199521912	0.1936966075	0.2798822515	0.3372790468
$H_0 : \rho = -0.6$	0.0730823926	0.1473271638	0.2356720284	0.2956555137
$H_0 : \rho = -0.7$	0.0224856154	0.0959718806	0.1858125779	0.2480296609
$H_0 : \rho = -0.8$	-0.0331161940	0.0375565141	0.1278502525	0.1918422051
$H_0 : \rho = -0.9$	-0.0986046809	-0.0340111814	0.0542664926	0.1198052466

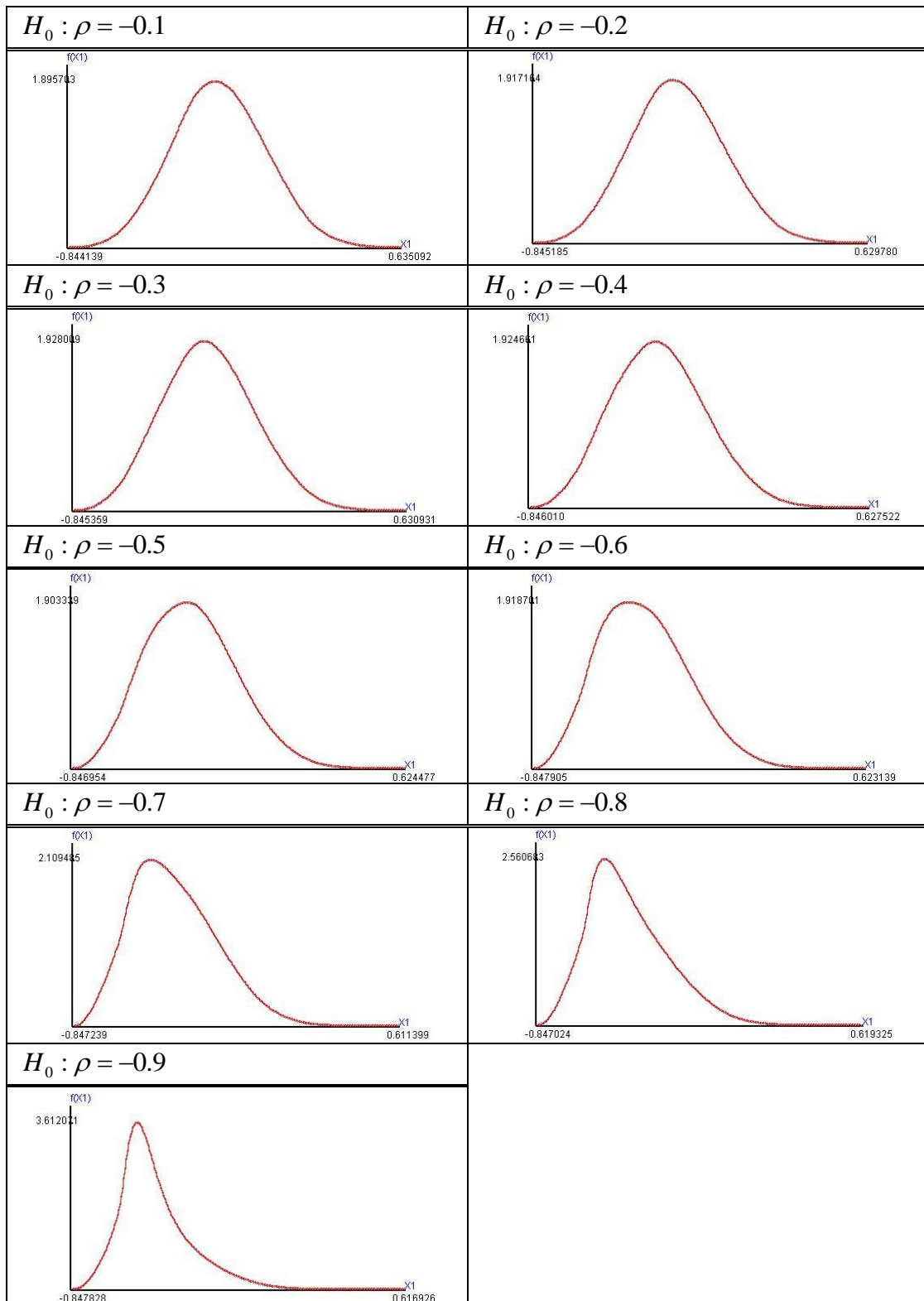
2.1.2)Case 2:

	X1	X2	X3
X4	X5	X6	
1 :	1.0342327801,	0.9938968730,	1.0055483431,
0.9972486251,	2.0174772521,	1.0011128268,	
2 :	1.9939250244,	2.0050617260,	2.0044291639,
1.9930661719,	3.9985932430,	1.9892018383,	
3 :	2.9946498749,	2.9993904712,	2.9862714459,
2.9938224367,	6.0303541935,	3.0053926267,	
4 :	3.9879783225,	3.9995636054,	3.9899215859,
4.0061246421,	7.9985945780,	4.0036825174,	
5 :	4.9886762254,	5.0123181307,	5.0038138429,
5.0014878150,	10.0058464462,	5.0035526421,	
6 :	6.0077623541,	5.9984657026,	5.9823589548,
5.9897260370,	11.9990123697,	6.0070164330,	
7 :	6.9986625588,	7.0025867488,	6.9999655244,
6.9759312192,	13.9906223629,	7.0050104001,	
8 :	8.0193319154,	8.0100625078,	7.9964579556,
8.0165849229,	16.0063624223,	8.0082168311,	
9 :	8.9979656598,	8.9957332920,	8.9939490876,
8.9903687453,	18.0079181999,	8.9820910361,	
10 :	10.0120610022,	10.0029708724,	10.0091567574,
9.9907976356,	19.9919782139,	9.9911175111,	
11 :	10.9937528012,	10.9866900333,	11.0003603762,
10.9943661350,	21.9969665824,	10.9993986415,	
12 :	12.0082464631,	12.0119475244,	12.0046919009,
11.9857603548,	24.0059617883,	12.0070996197,	
13 :	12.9930932431,	12.9983892508,	12.9801822530,
13.0089394821,	26.0056412905,	13.0150885144,	
14 :	14.0004243955,	13.9881921651,	13.9946459118,
14.0258401477,	27.9945778811,	13.9868505142,	
15 :	15.0026946305,	15.0192188278,	15.0092123876,
15.0132537299,	30.0007441110,	15.0016819903,	

independent sample correlation coefficient-----

	X1	X2	X3	X4	X5
X2	0.999998689	1			
X3	0.999998969	0.999999411	1		
X4	0.999998091	0.999998526	0.999998403	1	
X5	0.999999107	0.999999410	0.999999153	0.999998846	1
X6	0.999998693	0.999999362	0.999998667	0.999998542	0.999999504





The probability distribution of Durbin Watson test will be modified when the autocorrelation coefficient changed.

Coefficeint:

Hypothesis	Average	Variance	Coefficient of Skewed	Coefficient of Kurtosis
$H_0 : \rho = 0$	-0.13950	0.04349	0.08427	2.82851
$H_0 : \rho = 0.1$	-0.10496	0.04419	0.05493	2.81328
$H_0 : \rho = 0.2$	-0.07082	0.04509	0.02680	2.79110
$H_0 : \rho = 0.3$	-0.03686	0.04621	-0.00219	2.76129
$H_0 : \rho = 0.4$	-0.00291	0.04755	-0.03439	2.72358
$H_0 : \rho = 0.5$	0.03104	0.04909	-0.07241	2.67911
$H_0 : \rho = 0.6$	0.06472	0.05072	-0.11838	2.63162
$H_0 : \rho = 0.7$	0.09725	0.05231	-0.17289	2.58797
$H_0 : \rho = 0.8$	0.12685	0.05367	-0.23319	2.55647
$H_0 : \rho = 0.9$	0.15024	0.05464	-0.28999	2.54203
$H_0 : \rho = -0.1$	-0.17461	0.04295	0.11651	2.83765
$H_0 : \rho = -0.2$	-0.21043	0.04248	0.15320	2.84180
$H_0 : \rho = -0.3$	-0.24701	0.04199	0.19602	2.84271
$H_0 : \rho = -0.4$	-0.28435	0.04138	0.24721	2.84411
$H_0 : \rho = -0.5$	-0.32236	0.04045	0.31044	2.85405
$H_0 : \rho = -0.6$	-0.36096	0.03896	0.39224	2.89096
$H_0 : \rho = -0.7$	-0.40034	0.03644	0.50563	3.00047
$H_0 : \rho = -0.8$	-0.44148	0.03202	0.68135	3.31461
$H_0 : \rho = -0.9$	-0.48753	0.02392	1.01669	4.35778

Critical value:

Hypothesis	$1-\alpha$			
	0.995	0.99	0.975	0.95
$H_0 : \rho = 0$	-0.6450523625	-0.6035814680	-0.5386947208	-0.4790666987
$H_0 : \rho = 0.1$	-0.6206176254	-0.5772553254	-0.5097858802	-0.4482353494
$H_0 : \rho = 0.2$	-0.5961851917	-0.5514657557	-0.4817413801	-0.4185912252
$H_0 : \rho = 0.3$	-0.5724590484	-0.5264689292	-0.4547449832	-0.3902220794
$H_0 : \rho = 0.4$	-0.5499584648	-0.5025670511	-0.4289136755	-0.3632270192
$H_0 : \rho = 0.5$	-0.5287165397	-0.4800586991	-0.4044972593	-0.3375068047
$H_0 : \rho = 0.6$	-0.5089003415	-0.4591783990	-0.3816062993	-0.3130160978
$H_0 : \rho = 0.7$	-0.4912419466	-0.4399060575	-0.3605309766	-0.2901200812
$H_0 : \rho = 0.8$	-0.4760026609	-0.4235322881	-0.3422609443	-0.2697289837
$H_0 : \rho = 0.9$	-0.4648755851	-0.4113658920	-0.3283344172	-0.2539846206
$H_0 : \rho = -0.1$	-0.6690430968	-0.6300635708	-0.5679431562	-0.5106044220
$H_0 : \rho = -0.2$	-0.6918686029	-0.6560970213	-0.5971163031	-0.5424509505
$H_0 : \rho = -0.3$	-0.7132612000	-0.6807688390	-0.6258291417	-0.5738431451
$H_0 : \rho = -0.4$	-0.7325765822	-0.7035838170	-0.6533109574	-0.6041756797
$H_0 : \rho = -0.5$	-0.7494942402	-0.7238454068	-0.6784531472	-0.6327395453
$H_0 : \rho = -0.6$	-0.7634589098	-0.7407329740	-0.7000357156	-0.6583073907
$H_0 : \rho = -0.7$	-0.7735843607	-0.7532550393	-0.7166902117	-0.6788749756
$H_0 : \rho = -0.8$	-0.7785551326	-0.7599458674	-0.7265237001	-0.6920359282
$H_0 : \rho = -0.9$	-0.7759667000	-0.7574865638	-0.7252227925	-0.6929406765

Hypothesis	α			
	0.05	0.025	0.01	0.005
$H_0 : \rho = 0$	0.2080840812	0.2762354150	0.3544786670	0.4036379042
$H_0 : \rho = 0.1$	0.2446847685	0.3132460391	0.3882693026	0.4338646699
$H_0 : \rho = 0.2$	0.2830450373	0.3503788895	0.4208929179	0.4625988333
$H_0 : \rho = 0.3$	0.3223280178	0.3868135169	0.4519254664	0.4894467644
$H_0 : \rho = 0.4$	0.3616008690	0.4220013602	0.4808393561	0.5139158954
$H_0 : \rho = 0.5$	0.3996316447	0.4548655167	0.5070561965	0.5355295842
$H_0 : \rho = 0.6$	0.4349853155	0.4843971976	0.5297125821	0.5540031995
$H_0 : \rho = 0.7$	0.4659606225	0.5093567613	0.5483047115	0.5689640857
$H_0 : \rho = 0.8$	0.4908614245	0.5288227814	0.5623886551	0.5800781665
$H_0 : \rho = 0.9$	0.5080149384	0.5418512719	0.5715841712	0.5871952311
$H_0 : \rho = -0.1$	0.1729219153	0.2398775956	0.3199001736	0.3720320075
$H_0 : \rho = -0.2$	0.1381232105	0.2045639478	0.2846325492	0.3391216993

$H_0 : \rho = -0.3$	0.1025512101	0.1697823073	0.2491820629	0.3048576802
$H_0 : \rho = -0.4$	0.0656210347	0.1343358076	0.2136210685	0.2695567642
$H_0 : \rho = -0.5$	0.0268882098	0.0969688046	0.1774443163	0.2327569307
$H_0 : \rho = -0.6$	-0.0138588622	0.0570369180	0.1390365846	0.1945615616
$H_0 : \rho = -0.7$	-0.0574160253	0.0133902378	0.0962942389	0.1529261203
$H_0 : \rho = -0.8$	-0.1075679426	-0.0364292954	0.0468293759	0.1043991036
$H_0 : \rho = -0.9$	-0.1811763086	-0.1042482233	-0.0178076101	0.0411398041