

2.11)  $X_1, \dots, X_{10} \stackrel{iid}{\sim} \text{Cauchy}(\mu = 0, \sigma = 1)$ ,

$Y_1 = \text{The 1st order statistic of } (X_1, \dots, X_{10}) = X_{(1)}$ ,

$Y_2 = \text{The 2nd order statistic of } (X_1, \dots, X_{10}) = X_{(2)}$ ,

$Y_3 = \text{The 3rd order statistic of } (X_1, \dots, X_{10}) = X_{(3)}$ ,

$Y_4 = \text{The 4th order statistic of } (X_1, \dots, X_{10}) = X_{(4)}$ ,

$Y_5 = \text{The 5th order statistic of } (X_1, \dots, X_{10}) = X_{(5)}$ ,

$Y_6 = \text{The 6th order statistic of } (X_1, \dots, X_{10}) = X_{(6)}$ ,

$Y_7 = \text{The 7th order statistic of } (X_1, \dots, X_{10}) = X_{(7)}$ ,

$Y_8 = \text{The 8th order statistic of } (X_1, \dots, X_{10}) = X_{(8)}$ ,

$Y_9 = \text{The 9th order statistic of } (X_1, \dots, X_{10}) = X_{(9)}$ ,

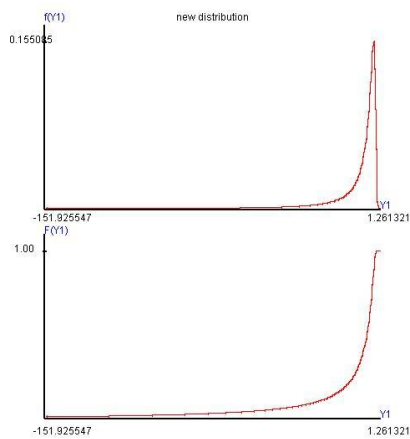
$Y_{10} = \text{The 10th order statistic of } (X_1, \dots, X_{10}) = X_{(10)}$

2.11.1)  $Y_1, \dots, Y_{10}$  probability distributions.

2.11.1.1)  $Y_1 = \text{The 1st order statistic of } (X_1, \dots, X_{10})$

$f_{Y_1}(y_1), F_{Y_1}(y_1)$

coefficient

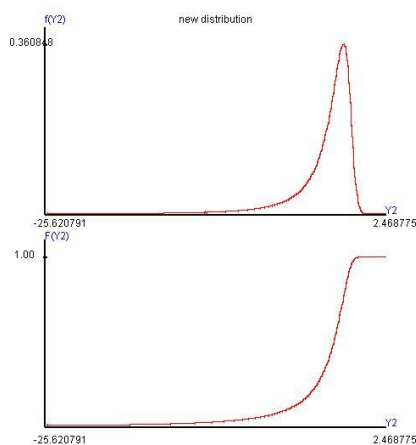


Mathematical Mean:	-11.65041
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	467.72262
S.D. :	21.62690
Skewed Coef. :	-4.45830
Kurtosis Coef. :	27.25733
MAD :	11.63241
Range :	201.55672
Mid_range :	-99.22131
Median :	-4.58624
Q1 :	-10.62937
Q2 :	-4.58624
Q3 :	-2.29888
IQR :	8.33049
C.V. :	none

2.11.1.2)  $Y_2 = \text{The 2nd order statistic of } (X_1, \dots, X_{10})$

$f_{Y_2}(y_2), F_{Y_2}(y_2)$

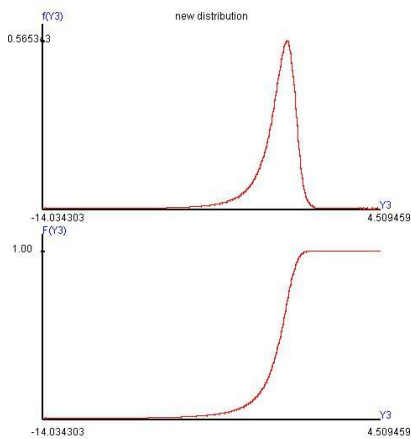
coefficient



Mathematical Mean:	-2.81774
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	17.54655
S.D. :	4.18886
Skewed Coef. :	-9.23081
Kurtosis Coef. :	173.06455
MAD :	2.07413
Range :	201.47599
Mid_range :	-98.21499
Median :	-1.77493
Q1 :	-3.15537
Q2 :	-1.77493
Q3 :	-1.01181
IQR :	2.14356
C.V. :	none

2.11.1.3)  $Y_3 = \text{The 3rd order statistic of } (X_1, \dots, X_{10})$

$f_{Y_3}(y_3), F_{Y_3}(y_3)$

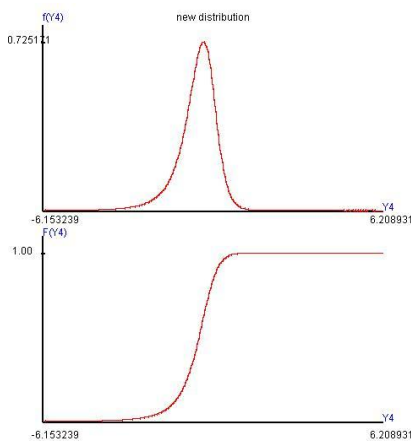


coefficient

Mathematical Mean:	-1.25794
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	2.01776
S.D. :	1.42048
Skewed Coef. :	-6.21435
Kurtosis Coef. :	131.62244
MAD :	0.86357
Range :	157.03813
Mid_range :	-73.97381
Median :	-0.94291
Q1 :	-1.61348
Q2 :	-0.94291
Q3 :	-0.48638
IQR :	1.12710
C.V. :	none

2.11.1.4)  $Y_4 = \text{The 4th order statistic of } (X_1, \dots, X_{10})$

$f_{Y_4}(y_4), F_{Y_4}(y_4)$

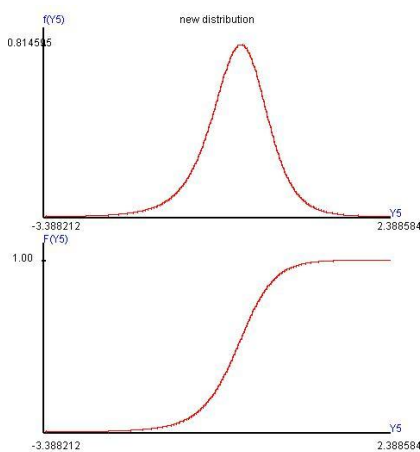


coefficient

Mathematical Mean:	-0.60847
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	0.62154
S.D. :	0.78838
Skewed Coef. :	-2.71528
Kurtosis Coef. :	36.18083
MAD :	0.54622
Range :	86.74660
Mid_range :	-37.14050
Median :	-0.48770
Q1 :	-0.92951
Q2 :	-0.48770
Q3 :	-0.13322
IQR :	0.79629
C.V. :	none

2.11.1.5)  $Y_5 = \text{The 5th order statistic of } (X_1, \dots, X_{10})$

$f_{Y_5}(y_5), F_{Y_5}(y_5)$

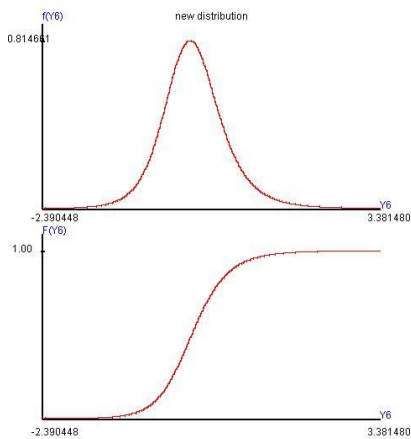


coefficient

Mathematical Mean:	-0.18550
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	0.36870
S.D. :	0.60721
Skewed Coef. :	-0.74932
Kurtosis Coef. :	9.17922
MAD :	0.44546
Range :	41.37531
Mid_range :	-8.14135
Median :	-0.15238
Q1 :	-0.50493
Q2 :	-0.15238
Q3 :	0.17561
IQR :	0.68054
C.V. :	none

2.11.1.6)  $Y_6 = \text{The 6th order statistic of } (X_1, \dots, X_{10})$

$f_{Y_6}(y_6), F_{Y_6}(y_6)$

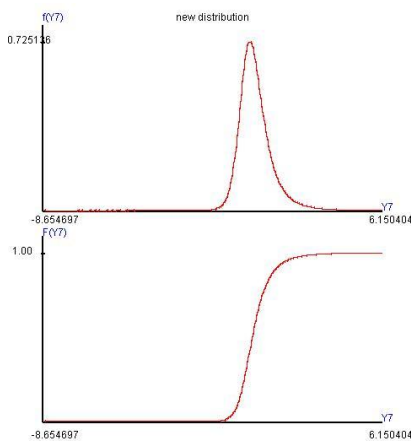


coefficient

Mathematical Mean:	0.18553
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	0.36864
S.D. :	0.60715
Skewed Coef. :	0.75015
Kurtosis Coef. :	10.23760
MAD :	0.44549
Range :	74.08478
Mid_range :	21.31695
Median :	0.15247
Q1 :	-0.17558
Q2 :	0.15247
Q3 :	0.50506
IQR :	0.68064
C.V. :	3.27262

2.11.1.7)  $Y_7 = \text{The 7th order statistic of } (X_1, \dots, X_{10})$

$f_{Y_7}(y_7), F_{Y_7}(y_7)$

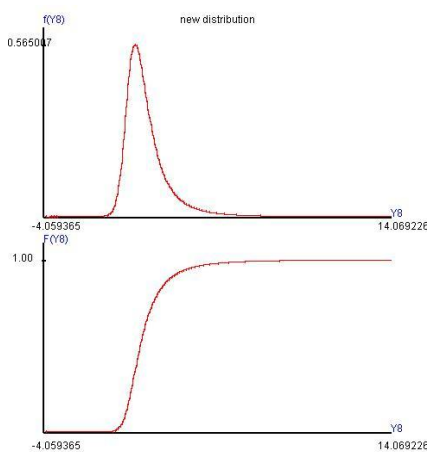


coefficient

Mathematical Mean:	0.60863
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	0.62145
S.D. :	0.78832
Skewed Coef. :	2.72782
Kurtosis Coef. :	40.33142
MAD :	0.54629
Range :	114.21831
Mid_range :	48.42588
Median :	0.48786
Q1 :	0.13334
Q2 :	0.48786
Q3 :	0.92964
IQR :	0.79630
C.V. :	1.29524

2.11.1.8)  $Y_8 = \text{The 8th order statistic of } (X_1, \dots, X_{10})$

$f_{Y_8}(y_8), F_{Y_8}(y_8)$

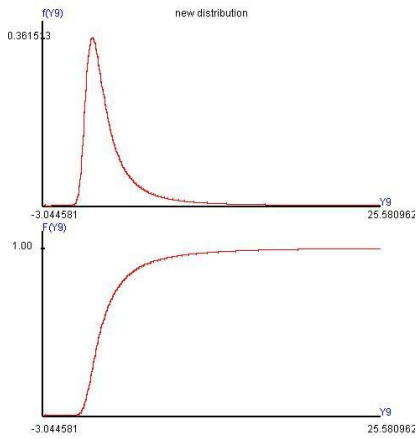


coefficient

Mathematical Mean:	1.25808
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	2.01917
S.D. :	1.42098
Skewed Coef. :	6.25841
Kurtosis Coef. :	137.36983
MAD :	0.86372
Range :	136.12041
Mid_range :	63.96584
Median :	0.94298
Q1 :	0.48638
Q2 :	0.94298
Q3 :	1.61361
IQR :	1.12723
C.V. :	1.12948

2.11.1.9)  $Y_9 = \text{The 9th order statistic of } (X_1, \dots, X_{10})$

$f_{Y_9}(y_9), F_{Y_9}(y_9)$

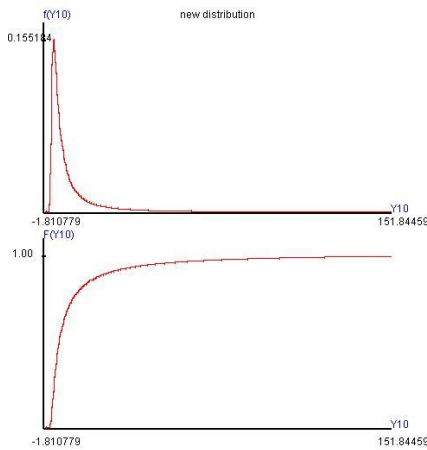


coefficient

Mathematical Mean:	2.81655
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	17.40492
S.D. :	4.17192
Skewed Coef. :	9.08649
Kurtosis Coef. :	167.26874
MAD :	2.07269
Range :	202.06720
Mid_range :	97.93376
Median :	1.77490
Q1 :	1.01154
Q2 :	1.77490
Q3 :	3.15543
IQR :	2.14390
C.V. :	1.48122

2.11.1.10)  $Y_{10} = \text{The 10th order statistic of } (X_1, \dots, X_{10})$

$f_{Y_{10}}(y_{10}), F_{Y_{10}}(y_{10})$



coefficient

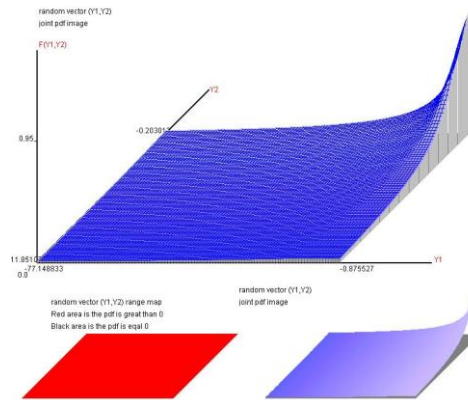
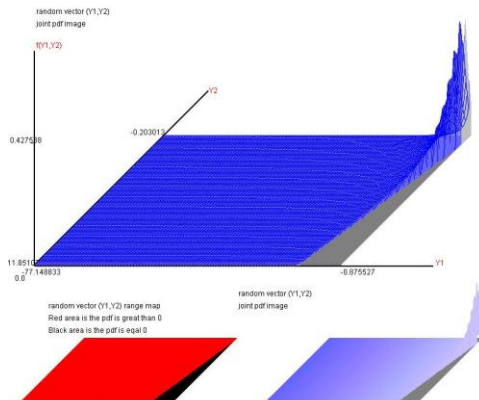
Mathematical Mean:	11.64857
Geometrical Mean :	none
Harmonic Mean :	none
Variance :	467.44210
S.D. :	21.62041
Skewed Coef. :	4.45714
Kurtosis Coef. :	27.24430
MAD :	11.63036
Range :	202.10730
Mid_range :	98.94624
Median :	4.58558
Q1 :	2.29851
Q2 :	4.58558
Q3 :	10.62963
IQR :	8.33112
C.V. :	1.85606

2.11.1.11)  $Y_1 = \text{The 1st order statistic of } (X_1, \dots, X_{10}),$

$Y_2 = \text{The 2nd order statistic of } (X_1, \dots, X_{10})$

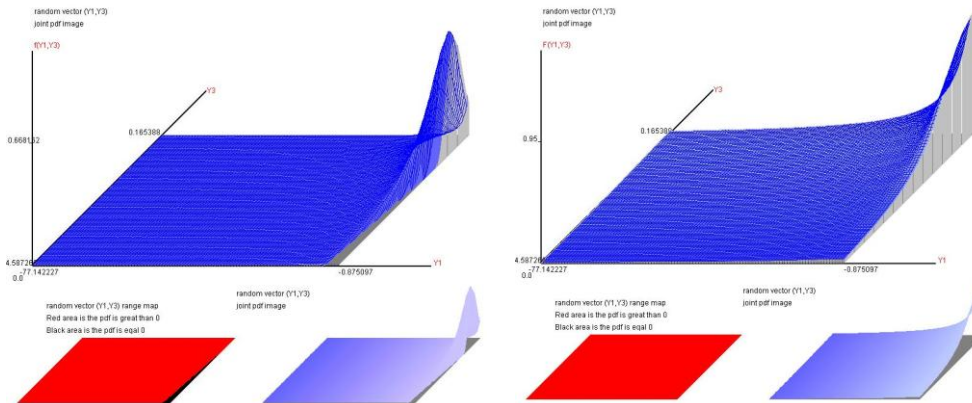
$f(y_1, y_2)$

$F(y_1, y_2)$



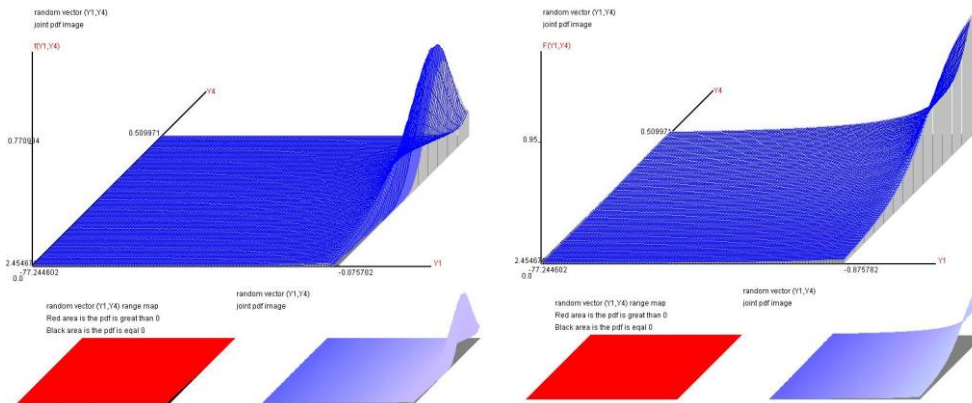
$E(Y_1) = -11.6502, \text{Var}(Y_1) = 467.7476$   
 $E(Y_2) = -2.8173, \text{Var}(Y_2) = 17.5287$   
 $\text{Cov}(Y_1, Y_2) = 36.9904,$   
 $Y_1 \text{ and } Y_2 \text{ correlation coefficient} = 0.4085.$

2.11.1.12)  $Y_1 = \text{The 1st order statistic of } (X_1, \dots, X_{10}),$   
 $Y_3 = \text{The 3rd order statistic of } (X_1, \dots, X_{10})$   
 $f(y_1, y_3)$   $F(y_1, y_3)$



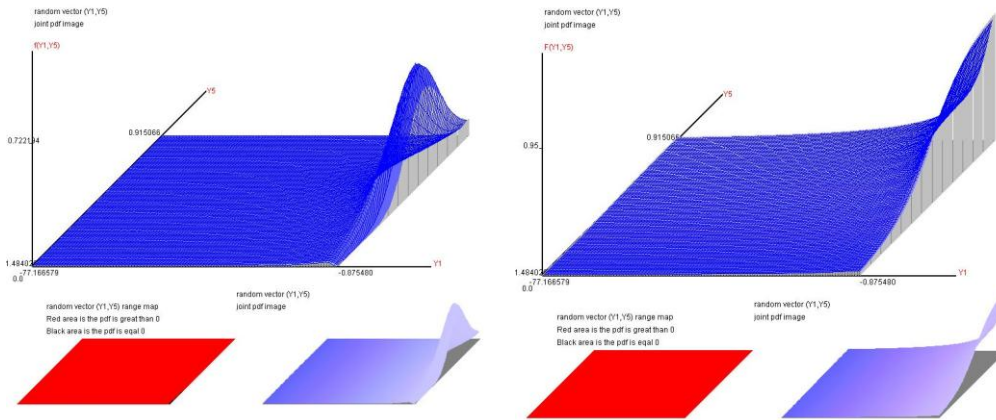
$E(Y_1) = -11.6506, \text{Var}(Y_1) = 467.6760$   
 $E(Y_3) = -1.2581, \text{Var}(Y_3) = 2.0253$   
 $\text{Cov}(Y_1, Y_3) = 8.3440,$   
 $Y_1 \text{ and } Y_3 \text{ correlation coefficient} = 0.2711.$

2.11.1.13)  $Y_1 = \text{The 1st order statistic of } (X_1, \dots, X_{10}),$   
 $Y_4 = \text{The 4th order statistic of } (X_1, \dots, X_{10})$   
 $f(y_1, y_4)$   $F(y_1, y_4)$



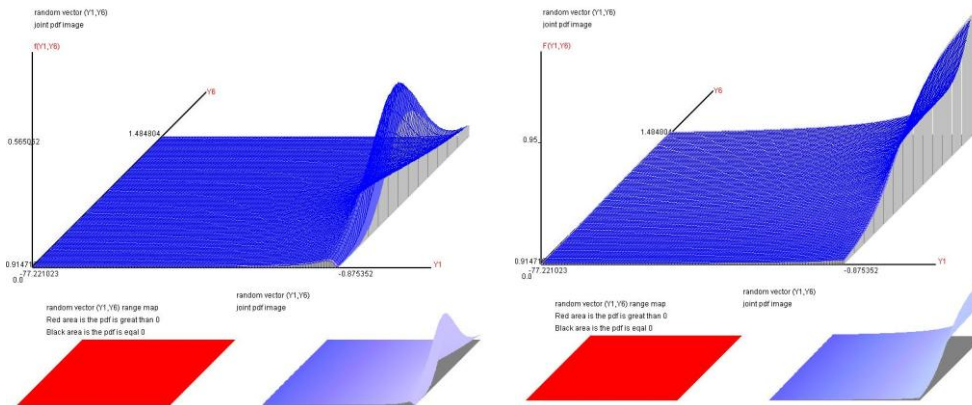
$E(Y_1) = -11.6501, \text{Var}(Y_1) = 467.6395$   
 $E(Y_4) = -0.6085, \text{Var}(Y_4) = 0.6213$   
 $\text{Cov}(Y_1, Y_4) = 3.4963,$   
 $Y_1 \text{ and } Y_4 \text{ correlation coefficient} = 0.2051.$

2.11.1.14)  $Y_1 = \text{The 1st order statistic of } (X_1, \dots, X_{10}),$   
 $Y_5 = \text{The 5th order statistic of } (X_1, \dots, X_{10})$   
 $f(y_1, y_5)$   $F(y_1, y_5)$



$E(Y_1) = -11.6489, \text{Var}(Y_1) = 467.4709$   
 $E(Y_5) = -0.1855, \text{Var}(Y_5) = 0.3685$   
 $\text{Cov}(Y_1, Y_5) = 2.0761,$   
 $Y_1 \text{ and } Y_5 \text{ correlation coefficient} = 0.1582.$

2.11.1.15)  $Y_1 = \text{The 1st order statistic of } (X_1, \dots, X_{10}),$   
 $Y_6 = \text{The 6th order statistic of } (X_1, \dots, X_{10})$   
 $f(y_1, y_6)$   $F(y_1, y_6)$



$E(Y_1) = -11.6505, \text{Var}(Y_1) = 467.6887$   
 $E(Y_6) = 0.1855, \text{Var}(Y_6) = 0.3686$   
 $\text{Cov}(Y_1, Y_6) = 1.5715,$   
 $Y_1 \text{ and } Y_6 \text{ correlation coefficient} = 0.1197.$