

5) The maximum of samples that is transferred to the exponential.

$$X_1, \dots, X_n \stackrel{iid}{\sim} f_X(x),$$

$$n \times (1 - \text{Max}(F_X(X_1), \dots, F_X(X_n))) \xrightarrow{n \rightarrow \infty} \text{Shifted_exponential}(\lambda = 1, c = 0),$$

5.1) $X_1, \dots, X_n \stackrel{iid}{\sim} U(0,1)$

$$Z_1 = n \times (1 - \text{Max}(X_1, \dots, X_n))$$

5.1.1) n=10

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.90897 Geometrical Mean : 0.53446 Harmonic Mean : 0.02391 Variance : 0.68864 S.D. : 0.82985 Skewed Coef. : 1.51726 Kurtosis Coef. : 5.77855 MAD : 0.63721 Range : 8.24476 Mid_range : 4.12238 Median : 0.66954 Q1 : 0.28353 Q2 : 0.66954 Q3 : 1.29425 IQR : 1.01072 C.V. : 0.91295

5.1.2) n=50

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.95232 Geometrical Mean : 0.54772 Harmonic Mean : 0.03347 Variance : 0.82420 S.D. : 0.90785 Skewed Coef. : 1.73168 Kurtosis Coef. : 7.05739 MAD : 0.68360 Range : 12.00227 Mid_range : 6.00113 Median : 0.68137 Q1 : 0.28562 Q2 : 0.68137 Q3 : 1.33933 IQR : 1.05372 C.V. : 0.95331

5.1.3)n=100

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
	Mathematical Mean: 0.99008 Geometrical Mean : 0.55871 Harmonic Mean : 0.04043 Variance : 0.96071 S.D. : 0.98016 Skewed Coef. : 1.94060 Kurtosis Coef. : 8.53731 MAD : 0.72478 Range : 17.97619 Mid_range : 8.98809 Median : 0.69088 Q1 : 0.28730 Q2 : 0.69088 Q3 : 1.37678 IQR : 1.08948 C.V. : 0.98998

5.1.4)n=5000

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
	Mathematical Mean: 0.99774 Geometrical Mean : 0.56091 Harmonic Mean : 0.04320 Variance : 0.99125 S.D. : 0.99562 Skewed Coef. : 1.98583 Kurtosis Coef. : 8.87600 MAD : 0.73337 Range : 16.67623 Mid_range : 8.33812 Median : 0.69307 Q1 : 0.28727 Q2 : 0.69307 Q3 : 1.38419 IQR : 1.09692 C.V. : 0.99787

5.1.5)n=10000

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
	Mathematical Mean: 0.99854 Geometrical Mean : 0.56126 Harmonic Mean : 0.04496 Variance : 0.99509 S.D. : 0.99754 Skewed Coef. : 1.99317 Kurtosis Coef. : 8.94157 MAD : 0.73441 Range : 16.30753 Mid_range : 8.15377 Median : 0.69179 Q1 : 0.28807 Q2 : 0.69179 Q3 : 1.38630 IQR : 1.09823 C.V. : 0.99900

5.1.6)n=100000

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient																																
	<table> <tr><td>Mathematical Mean:</td><td>1.00128</td></tr> <tr><td>Geometrical Mean :</td><td>0.56446</td></tr> <tr><td>Harmonic Mean :</td><td>0.04999</td></tr> <tr><td>Variance :</td><td>0.99852</td></tr> <tr><td>S.D. :</td><td>0.99926</td></tr> <tr><td>Skewed Coef. :</td><td>1.99677</td></tr> <tr><td>Kurtosis Coef. :</td><td>8.98901</td></tr> <tr><td>MAD :</td><td>0.73553</td></tr> <tr><td>Range :</td><td>16.89026</td></tr> <tr><td>Mid_range :</td><td>8.44513</td></tr> <tr><td>Median :</td><td>0.69537</td></tr> <tr><td>Q1 :</td><td>0.28869</td></tr> <tr><td>Q2 :</td><td>0.69537</td></tr> <tr><td>Q3 :</td><td>1.39497</td></tr> <tr><td>IQR :</td><td>1.10628</td></tr> <tr><td>C.V. :</td><td>0.99799</td></tr> </table>	Mathematical Mean:	1.00128	Geometrical Mean :	0.56446	Harmonic Mean :	0.04999	Variance :	0.99852	S.D. :	0.99926	Skewed Coef. :	1.99677	Kurtosis Coef. :	8.98901	MAD :	0.73553	Range :	16.89026	Mid_range :	8.44513	Median :	0.69537	Q1 :	0.28869	Q2 :	0.69537	Q3 :	1.39497	IQR :	1.10628	C.V. :	0.99799
Mathematical Mean:	1.00128																																
Geometrical Mean :	0.56446																																
Harmonic Mean :	0.04999																																
Variance :	0.99852																																
S.D. :	0.99926																																
Skewed Coef. :	1.99677																																
Kurtosis Coef. :	8.98901																																
MAD :	0.73553																																
Range :	16.89026																																
Mid_range :	8.44513																																
Median :	0.69537																																
Q1 :	0.28869																																
Q2 :	0.69537																																
Q3 :	1.39497																																
IQR :	1.10628																																
C.V. :	0.99799																																

[This is the problem which is the floating format can compute the 100000 times of powerful that is belonged to the maximum]

5.1.2) $X_1, \dots, X_n \sim^{iid} \text{Shifted_exp_ontial}(1,0), F_X(x) = 1 - \exp(-x)$
 $Z_1 = n \times (1 - \text{Ma}(1 - \exp(-X_1), \dots, 1 - \exp(-X_n)))$

5.2.1)n=10

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.90900 Geometrical Mean : 0.53450 Harmonic Mean : 0.05781 Variance : 0.68864 S.D. : 0.82985 Skewed Coef. : 1.51751 Kurtosis Coef. : 5.78017 MAD : 0.63720 Range : 8.54301 Mid_range : 4.27150 Median : 0.66952 Q1 : 0.28359 Q2 : 0.66952 Q3 : 1.29443 IQR : 1.01084 C.V. : 0.91292

5.2.2)n=20

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.95232 Geometrical Mean : 0.54767 Harmonic Mean : 0.05697 Variance : 0.82440 S.D. : 0.90797 Skewed Coef. : 1.73272 Kurtosis Coef. : 7.06725 MAD : 0.68364 Range : 11.69944 Mid_range : 5.84972 Median : 0.68125 Q1 : 0.28560 Q2 : 0.68125 Q3 : 1.33930 IQR : 1.05369 C.V. : 0.95342

5.2.3)n=50

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.98037 Geometrical Mean : 0.55582 Harmonic Mean : 0.05889 Variance : 0.92462 S.D. : 0.96157 Skewed Coef. : 1.88790 Kurtosis Coef. : 8.14181 MAD : 0.71424 Range : 14.68154 Mid_range : 7.34077 Median : 0.68826 Q1 : 0.28682 Q2 : 0.68826 Q3 : 1.36718 IQR : 1.08036 C.V. : 0.98082

6) The minimum of samples that is transferred to the exponential.

$$X_1, \dots, X_n \stackrel{iid}{\sim} f_X(x),$$

$$n \times \text{Min}(F_X(X_1), \dots, F_X(X_n)) \xrightarrow{n \rightarrow \infty} \text{Shifted_exponential}(\lambda = 1, c = 0),$$

6.1) $X_1, \dots, X_n \stackrel{iid}{\sim} U(0,1)$

$$Z_1 = n \times \text{Min}(X_1, \dots, X_n)$$

6.1.1) n=10

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.90905 Geometrical Mean : 0.53454 Harmonic Mean : 0.04242 Variance : 0.68845 S.D. : 0.82973 Skewed Coef. : 1.51666 Kurtosis Coef. : 5.77615 MAD : 0.63714 Range : 8.49449 Mid_range : 4.24724 Median : 0.66974 Q1 : 0.28366 Q2 : 0.66974 Q3 : 1.29446 IQR : 1.01080 C.V. : 0.91274

6.1.2) n=20

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.95237 Geometrical Mean : 0.54766 Harmonic Mean : 0.05203 Variance : 0.82476 S.D. : 0.90816 Skewed Coef. : 1.73287 Kurtosis Coef. : 7.06385 MAD : 0.68377 Range : 12.47582 Mid_range : 6.23791 Median : 0.68107 Q1 : 0.28557 Q2 : 0.68107 Q3 : 1.33936 IQR : 1.05379 C.V. : 0.95358

6.1.3)n=50

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
	Mathematical Mean: 0.98030 Geometrical Mean : 0.55585 Harmonic Mean : 0.05059 Variance : 0.92381 S.D. : 0.96115 Skewed Coef. : 1.88576 Kurtosis Coef. : 8.12797 MAD : 0.71405 Range : 14.61330 Mid_range : 7.30665 Median : 0.68842 Q1 : 0.28688 Q2 : 0.68842 Q3 : 1.36712 IQR : 1.08024 C.V. : 0.98047

6.1.4)n=100

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
	Mathematical Mean: 0.99014 Geometrical Mean : 0.55860 Harmonic Mean : 0.05345 Variance : 0.96138 S.D. : 0.98050 Skewed Coef. : 1.94222 Kurtosis Coef. : 8.54794 MAD : 0.72489 Range : 17.27368 Mid_range : 8.63684 Median : 0.69079 Q1 : 0.28723 Q2 : 0.69079 Q3 : 1.37649 IQR : 1.08926 C.V. : 0.99026

6.1.5)n=1000

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
	Mathematical Mean: 0.99882 Geometrical Mean : 0.56029 Harmonic Mean : 0.06007 Variance : 0.99542 S.D. : 0.99771 Skewed Coef. : 1.99217 Kurtosis Coef. : 8.93264 MAD : 0.73451 Range : 16.23591 Mid_range : 8.11795 Median : 0.69366 Q1 : 0.28700 Q2 : 0.69366 Q3 : 1.38465 IQR : 1.09765 C.V. : 0.99889

6.1.6)n=10000

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
	Mathematical Mean: 0.99785
	Geometrical Mean : 0.55407
	Harmonic Mean : 0.06984
	Variance : 1.00030
	S.D. : 1.00015
	Skewed Coef. : 1.99970
	Kurtosis Coef. : 9.00652
	MAD : 0.73611
	Range : 16.15869
	Mid_range : 8.07935
	Median : 0.69033
	Q1 : 0.28576
	Q2 : 0.69033
	Q3 : 1.37936
IQR : 1.09360	
C.V. : 1.00230	

[This is the problem which is the floating format can compute the 100000 times of powerful that is belonged to the maximum]

6.1.2) $X_1, \dots, X_n \sim^{iid} \text{Shifted_exp_ontial}(1,0), F_x(x) = 1 - \exp(-x)$
 $Z_1 = n \times \text{Min}(1 - \exp(-X_1), \dots, 1 - \exp(-X_n))$

6.2.1)n=10

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.90896 Geometrical Mean : none Harmonic Mean : none Variance : 0.68858 S.D. : 0.82981 Skewed Coef. : 1.51703 Kurtosis Coef. : 5.77774 MAD : 0.63721 Range : 8.40207 Mid_range : 4.20104 Median : 0.66951 Q1 : 0.28352 Q2 : 0.66951 Q3 : 1.29436 IQR : 1.01084 C.V. : 0.91292

6.2.2)n=20

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.95228 Geometrical Mean : none Harmonic Mean : none Variance : 0.82431 S.D. : 0.90792 Skewed Coef. : 1.73246 Kurtosis Coef. : 7.06315 MAD : 0.68361 Range : 12.14498 Mid_range : 6.07249 Median : 0.68119 Q1 : 0.28561 Q2 : 0.68119 Q3 : 1.33925 IQR : 1.05363 C.V. : 0.95341

7) $X_1, \dots, X_n \stackrel{iid}{\sim} B(1, p)$,

the discrete random samples function transfers to the continuous random variables.

7.1) $p = 0.5, Z_1 = \sum_{i=1}^n \frac{X_i}{2^i} \xrightarrow{n \rightarrow \infty} Uniform(0,1)$,

7.1.1)n=2,

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.37496 Geometrical Mean : none Harmonic Mean : none Variance : 0.07814 S.D. : 0.27953 Skewed Coef. : 0.00012 Kurtosis Coef. : 1.63983 MAD : 0.25002 Range : 0.75000 Mid_range : 0.37500 Median : 0.25000 Q1 : 0.00000 Q2 : 0.25000 Q3 : 0.50000 IQR : 0.50000 C.V. : 0.74548

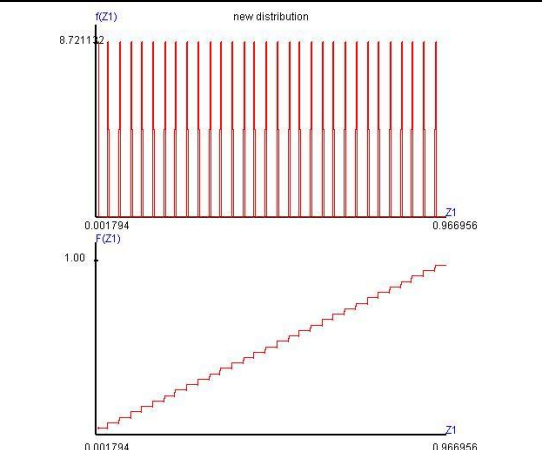
7.1.2)n=3,

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.43748 Geometrical Mean : none Harmonic Mean : none Variance : 0.08203 S.D. : 0.28641 Skewed Coef. : 0.00005 Kurtosis Coef. : 1.76195 MAD : 0.25000 Range : 0.87500 Mid_range : 0.43750 Median : 0.37500 Q1 : 0.12500 Q2 : 0.37500 Q3 : 0.62500 IQR : 0.50000 C.V. : 0.65468

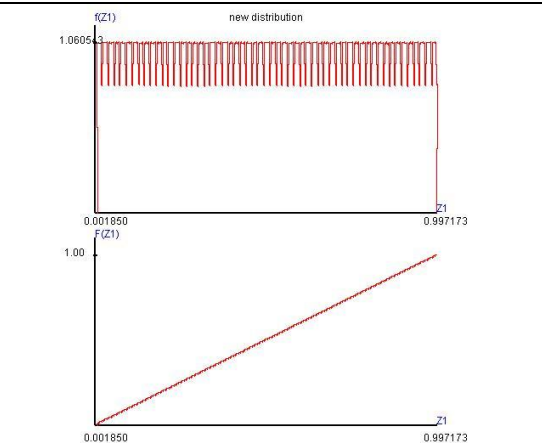
7.1.3)n=4,

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.46877 Geometrical Mean : none Harmonic Mean : none Variance : 0.08299 S.D. : 0.28808 Skewed Coef. : -0.00023 Kurtosis Coef. : 1.79084 MAD : 0.24996 Range : 0.93750 Mid_range : 0.46875 Median : 0.50000 Q1 : 0.25000 Q2 : 0.50000 Q3 : 0.68750 IQR : 0.43750 C.V. : 0.61454

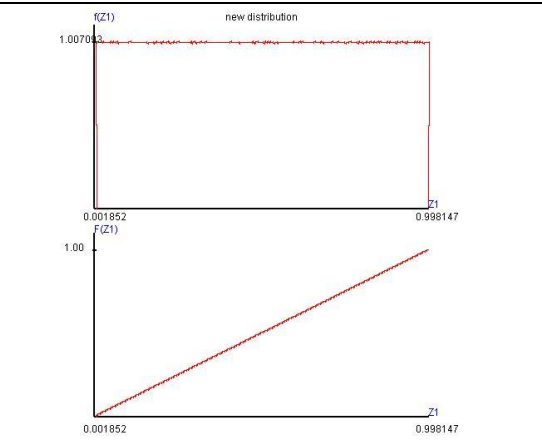
7.1.4)n=5,

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
 <p>The figure shows two plots for a uniform distribution with n=5. The top plot is a histogram with 5 bars, labeled 'new distribution', with a peak height of 8.721142. The x-axis ranges from 0.001794 to 0.966956. The bottom plot is the cumulative distribution function (CDF), labeled 'F(Z1)', showing a step function that increases from 0 to 1.00 over the same x-axis range.</p>	<p>Mathematical Mean: 0.48439 Geometrical Mean : none Harmonic Mean : none Variance : 0.08327 S.D. : 0.28856 Skewed Coef. : -0.00014 Kurtosis Coef. : 1.79746 MAD : 0.25003 Range : 0.96875 Mid_range : 0.48438 Median : 0.50000 Q1 : 0.21875 Q2 : 0.50000 Q3 : 0.75000 IQR : 0.53125 C.V. : 0.59572</p>

7.1.5)n=10,

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
 <p>The figure shows two plots for a uniform distribution with n=10. The top plot is a histogram with 10 bars, labeled 'new distribution', with a peak height of 1.06054. The x-axis ranges from 0.001850 to 0.997173. The bottom plot is the cumulative distribution function (CDF), labeled 'F(Z1)', showing a step function that increases from 0 to 1.00 over the same x-axis range.</p>	<p>Mathematical Mean: 0.49949 Geometrical Mean : none Harmonic Mean : none Variance : 0.08333 S.D. : 0.28867 Skewed Coef. : 0.00027 Kurtosis Coef. : 1.80003 MAD : 0.25000 Range : 0.99902 Mid_range : 0.49951 Median : 0.49902 Q1 : 0.24902 Q2 : 0.49902 Q3 : 0.74902 IQR : 0.50000 C.V. : 0.57794</p>

7.1.6)n=20,

$f_{z_1}(z_1), F_{z_1}(z_1)$	coefficient
 <p>The figure shows two plots for a uniform distribution with n=20. The top plot is a histogram with 20 bars, labeled 'new distribution', with a peak height of 1.007013. The x-axis ranges from 0.001852 to 0.998147. The bottom plot is the cumulative distribution function (CDF), labeled 'F(Z1)', showing a step function that increases from 0 to 1.00 over the same x-axis range.</p>	<p>Mathematical Mean: 0.49999 Geometrical Mean : none Harmonic Mean : none Variance : 0.08334 S.D. : 0.28869 Skewed Coef. : 0.00005 Kurtosis Coef. : 1.79985 MAD : 0.25002 Range : 1.00000 Mid_range : 0.50000 Median : 0.49996 Q1 : 0.24997 Q2 : 0.49996 Q3 : 0.75004 IQR : 0.50007 C.V. : 0.57739</p>

$$7.2) p = 0.1, Z_1 = \sum_{i=1}^n \frac{X_i}{2^i}$$

7.2.1)n=10,

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.09994 Geometrical Mean : none Harmonic Mean : none Variance : 0.03001 S.D. : 0.17325 Skewed Coef. : 1.97890 Kurtosis Coef. : 6.06393 MAD : 0.12764 Range : 0.99707 Mid_range : 0.49854 Median : 0.00781 Q1 : 0.00000 Q2 : 0.00781 Q3 : 0.12500 IQR : 0.12500 C.V. : 1.73357

7.2.2)n=20,

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.09996 Geometrical Mean : none Harmonic Mean : none Variance : 0.02998 S.D. : 0.17316 Skewed Coef. : 1.98000 Kurtosis Coef. : 6.06937 MAD : 0.12755 Range : 0.99609 Mid_range : 0.49805 Median : 0.00783 Q1 : 0.00008 Q2 : 0.00783 Q3 : 0.12502 IQR : 0.12494 C.V. : 1.73223

7.2.3)n=30,

$f_{Z_1}(z_1), F_{Z_1}(z_1)$	coefficient
	Mathematical Mean: 0.09996 Geometrical Mean : none Harmonic Mean : none Variance : 0.02999 S.D. : 0.17318 Skewed Coef. : 1.98026 Kurtosis Coef. : 6.06998 MAD : 0.12756 Range : 0.99222 Mid_range : 0.49611 Median : 0.00783 Q1 : 0.00008 Q2 : 0.00783 Q3 : 0.12502 IQR : 0.12494 C.V. : 1.73244

8) Population mean is zero and Sample variance is replaced by the sample variance.

$$8.1) X_1, \dots, X_n \stackrel{iid}{\sim} N(0,1), U_1 = \frac{\sqrt{n} \times \frac{X_1 + \dots + X_n}{n}}{\sqrt{\frac{X_1^2 + \dots + X_n^2}{n}}}$$

$$W_1 = \frac{X_1 + \dots + X_n}{\sqrt{X_1^2 + \dots + X_n^2}} \xrightarrow{n \rightarrow \infty} N(0,1),$$

8.1.1)n=10,

$f_{W_1}(w_1), F_{W_1}(w_1)$	coefficient
	Mathematical Mean: -0.00011 Geometrical Mean : none Harmonic Mean : none Variance : 1.00010 S.D. : 1.00005 Skewed Coef. : -0.00014 Kurtosis Coef. : 2.50038 MAD : 0.81805 Range : 6.21396 Mid_range : 0.00738 Median : 0.00006 Q1 : -0.72126 Q2 : 0.00006 Q3 : 0.72114 IQR : 1.44239 C.V. : none

8.1.2)n=20,

$f_{U_1}(u_1), F_{U_1}(u_1)$	coefficient
	Mathematical Mean: 0.00009 Geometrical Mean : none Harmonic Mean : none Variance : 1.00008 S.D. : 1.00004 Skewed Coef. : -0.00002 Kurtosis Coef. : 2.72754 MAD : 0.80790 Range : 8.14341 Mid_range : -0.04902 Median : 0.00010 Q1 : -0.69675 Q2 : 0.00010 Q3 : 0.69680 IQR : 1.39356 C.V. : none

8.1.3)n=30,

$f_{U_1}(u_1), F_{U_1}(u_1)$	coefficient
	Mathematical Mean: 0.00007 Geometrical Mean : none Harmonic Mean : none Variance : 0.99990 S.D. : 0.99995 Skewed Coef. : -0.00005 Kurtosis Coef. : 2.81316 MAD : 0.80450 Range : 9.06304 Mid_range : -0.10130 Median : -0.00001 Q1 : -0.68903 Q2 : -0.00001 Q3 : 0.68928 IQR : 1.37832 C.V. : none

8.1.4)n=50,

$f_{W_1}(w_1), F_{W_1}(w_1)$	coefficient
	Mathematical Mean: 0.00001 Geometrical Mean : none Harmonic Mean : none Variance : 0.99981 S.D. : 0.99991 Skewed Coef. : -0.00015 Kurtosis Coef. : 2.88459 MAD : 0.80182 Range : 9.74762 Mid_range : -0.00790 Median : 0.00021 Q1 : -0.68321 Q2 : 0.00021 Q3 : 0.68325 IQR : 1.36646 C.V. : none

8.1.5)n=100,

$f_{W_1}(w_1), F_{W_1}(w_1)$	coefficient
	Mathematical Mean: 0.00003 Geometrical Mean : none Harmonic Mean : none Variance : 1.00014 S.D. : 1.00007 Skewed Coef. : -0.00007 Kurtosis Coef. : 2.94143 MAD : 0.79991 Range : 10.41711 Mid_range : 0.04455 Median : -0.00002 Q1 : -0.67869 Q2 : -0.00002 Q3 : 0.67876 IQR : 1.35744 C.V. : none

$$8.2) X_1, \dots, X_n \stackrel{iid}{\sim} DE(1,0), W_1 = \sqrt{n} \times \frac{X_1 + \dots + X_n}{\sqrt{\frac{X_1^2 + \dots + X_n^2}{n}}}$$

$$= \frac{X_1 + \dots + X_n}{\sqrt{X_1^2 + \dots + X_n^2}} \xrightarrow{n \rightarrow \infty} N(0,1),$$

8.2.1)n=10,

$f_{w_1}(w_1), F_{w_1}(w_1)$	coefficient
	Mathematical Mean: 0.00010 Geometrical Mean : none Harmonic Mean : none Variance : 1.00001 S.D. : 1.00000 Skewed Coef. : -0.00002 Kurtosis Coef. : 2.33021 MAD : 0.82953 Range : 6.18036 Mid_range : -0.00719 Median : 0.00026 Q1 : -0.75325 Q2 : 0.00026 Q3 : 0.75350 IQR : 1.50675 C.V. : none

8.2.2)n=20,

$f_{w_1}(w_1), F_{w_1}(w_1)$	coefficient
	Mathematical Mean: -0.00033 Geometrical Mean : none Harmonic Mean : none Variance : 0.99994 S.D. : 0.99997 Skewed Coef. : 0.00026 Kurtosis Coef. : 2.58751 MAD : 0.81507 Range : 7.76282 Mid_range : -0.06583 Median : -0.00049 Q1 : -0.71540 Q2 : -0.00049 Q3 : 0.71469 IQR : 1.43009 C.V. : none

8.2.3)n=30,

$f_{w_1}(w_1), F_{w_1}(w_1)$	coefficient
	Mathematical Mean: 0.00037 Geometrical Mean : none Harmonic Mean : none Variance : 1.00003 S.D. : 1.00001 Skewed Coef. : -0.00035 Kurtosis Coef. : 2.69863 MAD : 0.80977 Range : 8.37798 Mid_range : 0.03206 Median : 0.00047 Q1 : -0.70133 Q2 : 0.00047 Q3 : 0.70218 IQR : 1.40351 C.V. : none

8.2.4)n=50,

$f_{w_1}(w_1), F_{w_1}(w_1)$	coefficient
	Mathematical Mean: -0.00052 Geometrical Mean : none Harmonic Mean : none Variance : 1.00012 S.D. : 1.00006 Skewed Coef. : 0.00083 Kurtosis Coef. : 2.80205 MAD : 0.80533 Range : 9.63583 Mid_range : 0.15905 Median : -0.00065 Q1 : -0.69181 Q2 : -0.00065 Q3 : 0.69064 IQR : 1.38245 C.V. : none

8.2.5)n=100,

$f_{w_1}(w_1), F_{w_1}(w_1)$	coefficient
	Mathematical Mean: -0.00076 Geometrical Mean : none Harmonic Mean : none Variance : 1.00000 S.D. : 1.00000 Skewed Coef. : 0.00112 Kurtosis Coef. : 2.89286 MAD : 0.80168 Range : 10.18602 Mid_range : -0.14167 Median : -0.00095 Q1 : -0.68374 Q2 : -0.00095 Q3 : 0.68193 IQR : 1.36567 C.V. : none

$$8.3) X_1, \dots, X_n \stackrel{iid}{\sim} \text{Arcsin}(0, 1.414213562), W_1 = \sqrt{n} \times \frac{X_1 + \dots + X_n}{\sqrt{\frac{X_1^2 + \dots + X_n^2}{n}}}$$

$$= \frac{X_1 + \dots + X_n}{\sqrt{X_1^2 + \dots + X_n^2}} \xrightarrow{n \rightarrow \infty} N(0, 1),$$

8.3.1)n=10,

$f_{W_1}(w_1), F_{W_1}(w_1)$	coefficient
	Mathematical Mean: -0.00009 Geometrical Mean : none Harmonic Mean : none Variance : 0.99993 S.D. : 0.99996 Skewed Coef. : 0.00005 Kurtosis Coef. : 2.69543 MAD : 0.80843 Range : 6.31997 Mid_range : -0.00077 Median : -0.00002 Q1 : -0.69749 Q2 : -0.00002 Q3 : 0.69727 IQR : 1.39476 C.V. : none

8.3.2)n=20,

$f_{W_1}(w_1), F_{W_1}(w_1)$	coefficient
	Mathematical Mean: 0.00001 Geometrical Mean : none Harmonic Mean : none Variance : 0.99999 S.D. : 1.00000 Skewed Coef. : -0.00002 Kurtosis Coef. : 2.84865 MAD : 0.80304 Range : 8.66698 Mid_range : -0.01717 Median : -0.00006 Q1 : -0.68559 Q2 : -0.00006 Q3 : 0.68570 IQR : 1.37129 C.V. : none

8.3.3)n=30,

$f_{w_1}(w_1), F_{w_1}(w_1)$	coefficient
	Mathematical Mean: 0.00002 Geometrical Mean : none Harmonic Mean : none Variance : 0.99986 S.D. : 0.99993 Skewed Coef. : -0.00019 Kurtosis Coef. : 2.89838 MAD : 0.80126 Range : 9.58347 Mid_range : 0.05146 Median : -0.00006 Q1 : -0.68187 Q2 : -0.00006 Q3 : 0.68190 IQR : 1.36377 C.V. : none

8.3.4)n=50,

$f_{w_1}(w_1), F_{w_1}(w_1)$	coefficient
	Mathematical Mean: 0.00003 Geometrical Mean : none Harmonic Mean : none Variance : 1.00004 S.D. : 1.00002 Skewed Coef. : -0.00035 Kurtosis Coef. : 2.94044 MAD : 0.79990 Range : 10.34975 Mid_range : 0.11891 Median : 0.00005 Q1 : -0.67873 Q2 : 0.00005 Q3 : 0.67882 IQR : 1.35755 C.V. : none

8.3.5)n=100,

$f_{w_1}(w_1), F_{w_1}(w_1)$	coefficient
	Mathematical Mean: 0.00002 Geometrical Mean : none Harmonic Mean : none Variance : 1.00007 S.D. : 1.00004 Skewed Coef. : -0.00001 Kurtosis Coef. : 2.96999 MAD : 0.79894 Range : 10.98688 Mid_range : -0.10972 Median : 0.00001 Q1 : -0.67673 Q2 : 0.00001 Q3 : 0.67668 IQR : 1.35341 C.V. : none